

# **Thermal Design**

Heat Transfer
Temperature Measurement
The prevalence of the number 5.7

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## **Chief Thermal Properties**

- · Thermal Conductivity
  - κ measured in W/m/K
  - heat flow (in W) is

 $P = \kappa \cdot \Delta T \cdot A/t$ 

- note that heat flow increases with increasing  $\Delta T$ , increasing surface area, and decreasing thickness (very intuitive)
- · Specific Heat Capacity
  - c<sub>n</sub> measured in J/kg/K
  - energy locked up in heat is:

 $E = c_D \cdot \Delta T \cdot m$ 

- energy stored proportional to  $\Delta T$ , and mass (intuitive)
- Emisivity, ε
  - power radiated is  $P = \varepsilon A \sigma T^4$

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# Why Care about Thermal?

- · Scientific equipment often needs temperature control
  - especially in precision measurement
- Want to calculate thermal energy requirements
  - how much energy to change temperature?
  - how much power to maintain temperature?
- Want to calculate thermal time constants
  - how long will it take to change the temperature?
- Want to understand relative importance of radiation, convection, conduction
  - which dominates?
  - how much can we limit/exaggerate a particular process?

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## **Thermal Conductivity of Materials**

· (copied from materials lecture)

Material	κ (W m <sup>-1</sup> K <sup>-1</sup> )	comments	
Silver	422	room T metals feel cold	
Copper	391	great for pulling away heat	
Gold	295		
Aluminum	205		
Stainless Steel	10–25	why cookware uses S.S.	
Glass, Concrete, Wood	0.5–3	buildings	
Many Plastics	~0.4	room T plastics feel warm	
G-10 fiberglass	0.29	strongest insulator choice	
Stagnant Air	0.024	but usually moving	
Styrofoam	0.01-0.03	can be better than air!	

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### Conduction: Heated Box

- A 1 m  $\times$  1 m  $\times$  2.5 m ice-fishing hut stands in the -10 $^{\circ}$ C cold with 2.5 cm walls of wood
  - $-A = 12 \text{ m}^2$
  - t = 0.025 m
  - $-\kappa \approx 1 \text{ W/m/K}$
- To keep this hut at 20° C would require

$$P = \kappa \cdot \Delta T \cdot A/t = (1.0)(30)(12)/(0.025) = 14,400 \text{ W}$$

- Outrageous!
- Replace wood with insulation:  $\kappa = 0.02$ : t = 0.025

$$P = \kappa \cdot \Delta T \cdot A/t = (0.02)(30)(12)/(0.025) = 288 \text{ W}$$

- This, we can do for less than \$40 at Target
- First example unfair
  - air won't carry heat away this fast: more on this later

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### R-value of insulation

- · In a hardware store, you'll find insulation tagged with an "R-value"
  - thermal resistance R-value is  $t/\kappa$
  - R-value is usually seen in imperial units: ft2·F·hr/Btu
  - Conversion factor is 5.67:
    - R-value of 0.025-thick insulation of  $\kappa$  = 0.02 W/m/K is:
      - $R = 5.67 \times t/\kappa = 5.67 \times 0.025/0.02 = 7.1$
  - Can insert Home-Depot R=5 insulation into formula:  $P = 5.67 \times A \cdot \Delta T/R$
  - so for our hut with R = 5:  $P \approx 5.67 \times (12)(30)/5 = 408$  W
  - note our earlier insulation example had R = 7.1 instead of 5, in which case P = 288 W (check for yourself!)

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## A Cold Finger

- Imagine a plug of aluminum connecting the inside to
  - how much will it change the story?
  - cylindrical shape, length t, radius R
  - $\kappa = 205 \text{ W/m/K}$
  - just based on conduction alone, since difference in thermal conductivity is a factor of 10,000, the cold finger is as important as the whole box if it's area is as big as 1/10,000 the area of the box.
  - this corresponds to a radius of 2 mm !!!
- So a cold finger can "short-circuit" the deliberate attempts at insulation
  - provided that heat can couple to it effectively enough: this will often limit the damage

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### Wikipedia on R-values:

- Note that these examples use the non-SI definition and are per inch. Vacuum insulated panel has the highest R-value of (approximately 45 in English units) for flat, Aerogel has the next highest R-value 10, followed by isocyanurate and phenolic foam insulations with, 8.3 and 7, respectively. They are followed closely by polyurethane and polystyrene insulation at roughly R-6 and R-5. Loose cellulose, fiberglass both blown and in batts, and rock wool both blown and in batts all possess an R-value of roughly 3. Straw bales perform at about R-1.45. Snow is roughly R-1.
- · Absolutely still air has an R-value of about 5 but this has little practical use: Spaces of one centimeter or greater will allow air to circulate, convecting heat and greatly reducing the insulating value to roughly R-1

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## Convective Heat Exchange

- Air (or any fluid) can pull away heat by physically transporting it
  - really conduction into fluid accompanied by motion of fluid
  - full, rigorous, treatment beyond scope of this class
- · General behavior:

power convected =  $P = h \cdot \Delta T \cdot A$ 

- A is area,  $\Delta T$  is temperature difference between surface and bath
- h is the convection coefficient, units: W/K/m<sup>2</sup>
- still air has  $h \approx 2-5 \text{ W/K/m}^2$ 
  - higher when  $\Delta T$  is higher: self-driven convective cells
  - note that h = 5.67 is equivalent to R = 1
- gentle breeze may have  $h \approx 5 10 \text{ W/K/m}^2$
- forced air may be several times larger ( $h \approx 10-50$ )

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### Radiative Heat Exchange

- · The Stephan-Boltzmann law tells us:
  - $-P = \varepsilon A \sigma (T_h^4 T_c^4)$
  - The Stephan-Boltzmann constant,  $\sigma$  = 5.67×10<sup>-8</sup> W/m<sup>2</sup>/K<sup>4</sup>
  - in thermal equilibrium  $(T_h = T_c)$ , there is radiative balance, and P = 0
  - the emissivity ranges from 0 (shiny) to 1 (black)
  - "black" in the thermal infrared band ( $\lambda \approx 10 \mu m$ ) might not be intuitive
    - your skin is nearly black ( $\varepsilon \approx 0.8$ )
    - plastics/organic stuff is nearly black ( $\varepsilon \approx 0.8-1.0$ )
    - · even white paint is black in the thermal infrared
    - · metals are almost the only exception
  - for small  $\Delta T$  around T,  $P \approx 4 \varepsilon A \sigma T^3 \Delta T = (4 \varepsilon \sigma T^3) \cdot A \cdot \Delta T$
  - which looks like convection, with  $h = 4\varepsilon\sigma T^3$
  - for room temperature,  $h \approx 5.7 \varepsilon$  W/K/m², so similar in magnitude to convection

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## **Convection Examples**

- Standing unclothed in a 20° C light breeze
  - $-h \approx 5 \text{ W/K/m}^2$
  - $\Delta T = 17^{\circ} \text{ C}$
  - $-A \approx 1 \text{ m}^2$
  - $-P \approx (5)(17)(1) = 85 \text{ W}$
- · Our hut from before:
  - $-h \approx 5 \text{ W/K/m}^2$
  - $-\Delta T = 30^{\circ}$  C (if the skin is at the hot temperature)
  - $A \approx 12 \text{ m}^2$
  - $-P \approx (5)(30)(12) = 1800 \text{ W}$

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## Radiative Examples

- Standing unclothed in room with -273° C walls
  - and assume emissivity is 0.8 for skin
  - $-A \approx 1 \text{ m}^2$
  - $-\Delta T = 310 \text{ K}$
  - $-P \approx (0.8)(1)(5.67 \times 10^{-8})(310^4) = 419 \text{ W (burr)}$
- Now bring walls to 20° C
  - $-\Delta T = 17^{\circ} \text{ C}$
  - $-P \approx (0.8)(1)(5.67 \times 10^{-8})(310^4 293^4) = 84 \text{ W}$
  - pretty similar to convection example
  - note that we brought our cold surface to 94.5% the absolute temperature of the warm surface, and only reduced the radiation by a factor of 5 (not a factor of 18): the fourth power makes this highly nonlinear

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### **Combined Problems**

- Two-layer insulation
  - must compute temperature at interface
- Conduction plus Convection
  - skin temperature must be solved
- Conduction plus Radiation
  - skin temperature must be solved
- · The whole enchilada
  - conduction, convection, radiation

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### **Conduction plus Convection**

- Let's take our hut with just wood, but considering convection
  - The skin won't necessarily be at Tout
  - Again, thermal equilibrium demands that power conducted through wall equals power wafted away in air
  - $-P = h \cdot (T_{skin} T_{out}) \cdot A = \kappa \cdot (T_{in} T_{skin}) \cdot A/t$
  - for which we find  $T_{skin} = (\kappa T_{in}/t + hT_{out})/(h + \kappa/t) = 16.7^{\circ}$  C
  - so the skin is hot
  - $-P = (5)(26.7)(12) \approx 1600 \text{ W}$
  - So a space heater actually could handle this (no radiation)
  - lesson: air could not carry heat away fast enough, so skin warms up until it can carry enough heat away—at the same time reducing ΔT across wood
  - h may tend higher due to self-induced airflow with large  $\Delta T$
  - also, a breeze/wind would help cool it off

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## Two-Layer insulation

- Let's take our ice-fishing hut and add insulation instead of replacing the wood with insulation
  - each still has thickness 0.025 m; and surface area 12 m<sup>2</sup>
  - Now have three temperatures:  $T_{in} = 20^{\circ}$ ,  $T_{midt}$ ,  $T_{out} = -10^{\circ}$
  - Flow through first is:  $P_1 = \kappa_1 \cdot (T_{in} T_{mid}) \cdot A_1/t_1$
  - Flow through second is:  $P_2 = \kappa_2 \cdot (T_{mid} T_{out}) \cdot A_2 / t_2$
  - In thermal equilibrium, must have  $P_1 = P_2$ 
    - · else energy is building up or coming from nowhere
  - We know everything but  $T_{mid}$ , which we easily solve for:
    - $T_{mid}(\kappa_1 A_1/t_1 + \kappa_2 A_2/t_2) = \kappa_2 A_2 T_{in}/t_2 + \kappa_2 A_2 T_{out}/t_2$
  - find  $T_{mid}$  = -9.412 or  $T_{mid}$  = 19.412 depending on which is interior or exterior
  - heat flow is 282 W (compare to 288 W before: wood hardly matters)

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## Convection plus Radiation

- How warm should a room be to stand comfortably with no clothes?
  - assume you can put out P = 100 W metabolic power
    - 2000 kcal/day = 8,368,000 J in 86400 sec ≈ 100 W
  - $-P = h \cdot (T_{skin} T_{out}) \cdot A + \varepsilon A \sigma (T_{skin}^4 T_{out}^4) \approx (hA + 4\varepsilon A \sigma T^3) \Delta T$
  - with emissivity = 0.8, T = 293 K
  - $-100 = ((5)(1) + 4.56)\Delta T$
  - $-\Delta T = 10.5^{\circ}$
  - so the room is about 310 10.5 = 299.5 K = 26.5° C = 80° F
  - iterating (using T = 299.5); 4.56 → 4.87;  $\Delta T$  → 10.1°
  - assumes skin is full internal body temperature
    - some conduction in skin reduces skin temperature
    - · so could tolerate slightly cooler

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#### The whole enchilada

- Let's take a cubic box with a heat source inside and consider all heat transfers
  - P = 1 W internal source
  - inside length = 10 cm
  - thickness = 2.5 cm
  - R-value = 5
  - so 5.67× $t/\kappa$  = 5 →  $\kappa$  = 0.028 W/m/K
  - effective conductive area is 12.5 cm cube  $\rightarrow A_c = 0.09375 \text{ m}^2$
  - external (radiative, convective) area is 15 cm cube  $\rightarrow$   $A_{\rm ext}$  = 0.135 m<sup>2</sup>
  - assume  $h = 5 \text{ W/K/m}^2$ ,  $\varepsilon = 0.8$ ,  $T_{ext} = 293 \text{ K}$
  - assume the air inside is thoroughly mixed (perhaps 1 W source is a fan!)

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#### The enchilada calculation

 power generated = power conducted = power convected plus power radiated away

 $P = \kappa \cdot (T_{in} - T_{skin}) \cdot A_c / t = (hA_{ext} + 4\varepsilon A_{ext} \sigma T^3) \cdot (T_{skin} - T_{ext})$ 

- first get T<sub>skin</sub> from convective/radiative piece
- $-T_{\text{skin}} = T_{\text{ext}} + P/(hA_{\text{ext}} + 4\varepsilon A_{\text{ext}}\sigma T^3) = 20^{\circ} + 1.0/(0.675 + 0.617)$
- $-T_{\rm skin} = 20.8^{\circ}$  (barely above ambient)
- now the  $\Delta T$  across the insulation is  $P \cdot t/(A_c \cdot \kappa) = 9.5^\circ$
- so  $T_{\rm in} = 30.3^{\circ}$
- Notice a few things:
  - radiation and convection nearly equal influence (0.617 vs. 0.675)
  - shutting off either would result in small (but measurable) change

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### **Timescales**

- So far we've looked at steady-state equilibrium situations
- How long will it take to "charge-up" the system?
- Timescale given by heat capacity times temperature change divided by power
  - $-\tau \approx c_p \cdot m \cdot \Delta T/P$
- For ballpark, can use c<sub>p</sub> ≈ 1000 J/kg/K for just about anything
  - so the box from before would be 2.34 kg if it had the density of water; let's say 0.5 kg in truth
  - average charge is half the total ∆T, so about 5°
  - total energy is (1000)(0.5)(5) = 2500 J
  - at 1W, this has a 40 minute timescale

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# Heating a lump by conduction

- Heating food from the outside, one relies entirely on thermal conduction/diffusion to carry heat in
- Relevant parameters are:
  - thermal conductivity, κ (how fast does heat move) (W/m/K)
  - heat capacity, c<sub>n</sub> (how much heat does it hold) (J/kg/K)
  - mass, m (how much stuff is there) (kg)
  - size, R—like a radius (how far does heat have to travel) (m)
- Just working off units, derive a timescale:
  - $-\tau \approx (c_{\rm p}/\kappa)(m/R) \approx 4(c_{\rm p}/\kappa)\rho R^2$
  - where  $\rho$  is density, in kg/m<sup>3</sup>:  $\rho \approx m/((4/3)\pi R^3) \approx m/4R^3$
  - faster if:  $c_0$  is small,  $\kappa$  is large, R is small (these make sense)
  - for typical food values,  $\tau \approx 6$  minutes × (R/1 cm)<sup>2</sup>
  - egg takes ten minutes, turkey takes 5 hours

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## Lab Experiment

 We'll build boxes with a heat load inside to test the ideas here

- In principle, we can:
  - measure the thermal conductivity of the insulation
  - see the impact of emissivity changes
  - see the impact of enhanced convection
  - look for thermal gradients in the absence of circulation
  - look at the impact of geometry on thermal state
  - see how serious heat leaks can be
- Nominal box:
  - 10 cm side, 1-inch thick, about 1.5 W (with fan)

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## Lab Experimental Suite

experiment	R	int. airflow	ext. airflow	int. foil	ext. foil	geom.
A (control)	25 Ω	1 fan	none	no	no	10 cm cube
B (ext. convec)	25 Ω	1 fan	fan	no	no	10 cm cube
C (ext. radiation)	25 Ω	1 fan	none	no	yes	10 cm cube
D (ext. conv/rad)	25 Ω	1 fan	fan	no	yes	10 cm cube
E (gradients)	25 Ω	none	none	no	no	10 cm cube
F (int. radiation)	25 Ω	1 fan	none	yes	no	10 cm cube
G (radiation)	25 Ω	1 fan	none	yes	yes	10 cm cube
H (more power)	12 Ω	1 fan	none	no	no	10 cm cube
I (larger area)	12 Ω	2 fans	none	no	no	17.5 cm cube
J (area and thick.)	12 Ω	2 fans	none	no	no	17.5 cm cube

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## Lab Experiment, cont.

- We'll use power resistors rated at 5 W to generate the heat
  - $-25 \Omega$  nominal
  - $-P = V^2/R$
  - At 5 V, nominal value is 1 W
  - can go up to 11 V with these resistors to get 5 W
  - a 12  $\Omega$  version puts us a bit over 2 W at 5 V
- Fans to circulate
  - small fans operating at 5 V (and about 0.5 W) will keep the air moving
- Aluminum foil tape for radiation control
  - several varieties available
- · Standard building insulation

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### Temperature measurement

- · There are a variety of ways to measure temperature
  - thermistor
  - RTD (Resistive Temperature Device)
  - AD-590
  - thermocouple
- Both the thermistor and RTD are resistive devices
  - thermistor not calibrated, nonlinear, cheap, sensitive
  - platinum RTDs accurate, calibrated, expensive
- We'll use platinum RTDs for this purpose
  - small: very short time constant
  - accurate: no need to calibrate
  - measure with simple ohm-meter
  - $-R = 1000.0 + 3.85 \times (T 0^{\circ}C)$ 
    - so 20°C would read 1077.0  $\Omega$

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#### Random Notes

- Rig fan and resistor in parallel, running off 5V
  - fan can accept range: 4.5-5.5 V
  - if you want independent control, don't rig together
- · Use power supply current reading (plus voltage) to ascertain power (P = IV) being delivered into box
- · Make sure all RTDs read same thing on block of thermally stabilized chunk of metal
  - account for any offset in analysis
- · Don't let foil extend to outside as a cold finger
- · Make sure you have no air gaps: tape inside and out of seams
  - but need to leave top accessible
  - nice to tape fan to top (avoid heat buildup here)
  - can hang resistor, RTD from top as well (easy to assemble)

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### Random Notes, continued

- Measure temp. every ~2 minutes initially
  - tie white leads of RTDs to common DVM all together
  - label red lead so you know where it goes
- · After equilibrium is reached, measure skin temperatures
  - hold in place with spare foam (not finger or thermal conductor!)
  - best to note time of each digit change
    - · allows extrapolation to final (slow otherwise)
- We have limited RTDs, so 3-4 per group will be standard
  - locate inside RTD in fan exhaust, so representative
  - use external RTD for ambient, skin (double duty)
  - some experiments will want more RTDs (gradients)
- · Once equilibrated, go to configuration B
  - turn on external fan, coat with foil, poke a hole, cold finger

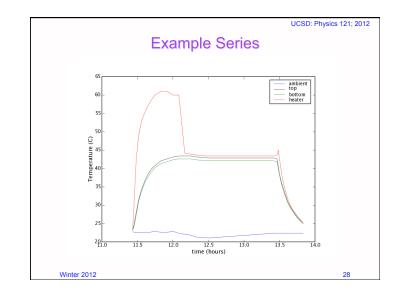
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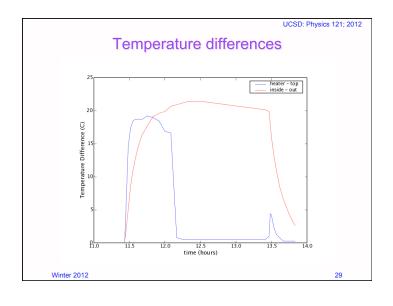
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### Random Notes, continued

- · Send your data points to me via e-mail so I can present the amalgam of results to the class
  - use format:
    - hh:mm RTD1 RTD2 RTD3 etc.
  - example:
    - 11:43 1088 1155 1152 1228
  - include a description of what each column represents
- Also include basic setup and changes in e-mail so I know what I'm plotting
- Also include in the message temperatures you measure only once, or occasionally (like skin temp.)
- · I'll make the data available for all to access for the write-ups

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UCSD: Physics 121; 2012 References and Assignment Useful text: - Introduction to Heat Transfer: Incropera & DeWitt Reading in text: - Chapter 8 (7 in 3rd ed.) reading assignment: check web page for details

UCSD: Physics 121; 2012 Thermal Building Design You can get R-values for common construction materials online - see http://www.coloradoenergy.org/procorner/stuff/r-values.htm • Recall that  $R = 5.67 \times t/\kappa$ - so power,  $P = 5.67A\Delta T/R$ • Composite structures (like a wall) get a net R-value - some parts have insulation, some parts just studs - if we have two areas,  $A_1$  with  $R_1$  and  $A_2$  with  $R_2$ , total power is  $P = 5.67A_1\Delta T/R_1 + 5.67A_2\Delta T/R_2$ - so we can define net R so that it applies to  $A_{tot} = A_1 + A_2$  $-1/R_{\text{tot}} = (A_1/A_{\text{tot}})/R_1 + (A_2/A_{\text{tot}})/R_2$ - in example on web site, studs take up 15%, rest of wall 85%  $-P = 5.67A_{tot}\Delta T/R_{tot}$ Winter 2012

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## Handling External Flow as R-value

- On the materials site, they assign R-values to the air "layer" up against the walls
  - outside skin R = 0.17

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- inside skin R = 0.68
- This accounts for both convection and radiation. How?
  - recall that power through the walls has to equal the power convected and radiated

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P = 5.67A(T_{in}-T_{skin})/R = h_{conv}A(T_{skin}-T_{out}) + h_{rad}A(T_{skin}-T_{out})
P = 5.67A(T_{in}-T_{skin})/R = h_{eff}A(T_{skin}-T_{out})
```

- where  $h_{\rm rad} \approx 4\sigma\varepsilon T^3$ , and  $h_{\rm eff} = h_{\rm conv} + h_{\rm rad}$
- We can solve this for  $T_{\rm skin}$ , to find  $T_{\text{skin}} = (5.67T_{\text{in}}/R + h_{\text{eff}}T_{\text{out}})/(5.67/R + h_{\text{eff}})$

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# **Putting Together**

 Inserting the expression for T<sub>skin</sub> into the conduction piece, we get:

 $P = 5.67A(T_{\rm in} - T_{\rm skin})/R = 5.67A(T_{\rm in} - (5.67T_{\rm in}/R + h_{\rm eff}T_{\rm out})/(5.67/R + h_{\rm eff}))/R$ 

- multiply the solitary  $T_{\rm in}$  by  $(5.67/R+h_{\rm eff})/(5.67/R+h_{\rm eff})$
- 5.67T<sub>in</sub>/R term cancels out

 $P = 5.67A((h_{\text{eff}}T_{\text{in}} - h_{\text{eff}}T_{\text{out}})/(5.67/R + h_{\text{eff}}))/R$ 

 $P = 5.67A(T_{in}-T_{out}) \times h_{eff}/(5.67+h_{eff}R)$ 

 which now looks like a standard conduction relation between inside and outside temperatures, with an effective R:

 $R_{\rm eff} = R + 5.67/h_{\rm eff}$ 

- The effective R is the R-value of the original wall plus a piece from the air that looks like 5.67/h<sub>eff</sub>
  - the site has interior air layer  $R_{\rm eff}$ =0.68, or  $h_{\rm eff}$  = 8.3, which is appropriate for radiation plus convection
  - for exterior, they use  $R_{\rm eff}$  = 0.17, or  $h_{\rm eff}$  = 33, representing windy conditions

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## Dealing with the Ceiling

- The  $G_{ceil}$  and  $G_{roof}$  require interpretation, since the  $\Delta T$  across these interfaces is not the full  $\Delta T$  between inside and outside
  - there is a T<sub>attic</sub> in between
  - but we know that the heat flow through the ceiling must equal the heat flow through the roof, in equilibrium
  - so  $G_{ceil}(T_{in}-T_{attic}) = G_{roof}(T_{attic}-T_{out})$
  - then  $T_{\text{attic}} = (G_{\text{ceil}}T_{\text{in}} + G_{\text{roof}}T_{\text{out}})/(G_{\text{ceil}} + G_{\text{roof}})$
  - so that  $G_{ceil}(T_{in}-T_{attic}) = G_{up}(T_{in}-T_{out})$
  - where  $G_{up} = G_{ceil}G_{roof}/(G_{ceil}+G_{roof})$ , in effect acting like a parallel combination
- So G<sub>up</sub> evaluates to:
  - G<sub>up</sub> = 214, 74, 66, 42 for no/no, ceil/no, no/roof, ceil/roof insulation combinations

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#### A model house

- Ignoring the floor, let's compute the heat load to keep a house some ΔT relative to outside
  - useful to formulate  $G = P/\Delta T$  in W/K as property of house
  - Assume approx 40×40 ft floorplan (1600 ft²)
  - 8 feet tall, 20% windows on wall
  - Wall: 100 m<sup>2</sup>, windows: 20 m<sup>2</sup>, ceiling: 150 m<sup>2</sup>, roof 180 m<sup>2</sup>
- Can assess for insulation or not, different window choices, etc.
  - G<sub>window</sub> = 125, 57, 29 for single, double, or deluxe window
  - G<sub>wall</sub> = 142, 47 for no insul, insul
  - $-G_{ceil}$  = 428, 78 for no insul, insul
  - $-G_{roof} = 428$ , 90 for no insul, insul

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## All Together Now

- The total power required to stabilize the house is then
   P<sub>tot</sub> = G<sub>tot</sub> ΔT, where G<sub>tot</sub> = G<sub>windrow</sub> + G<sub>wall</sub> + G<sub>un</sub>
- For a completely uninsulated house:
  - $G_{tot} = 481 \text{ W/K}$
  - requires 7.2 kW to maintain  $\Delta T = 15^{\circ}C$
  - over 5 months (153 days), this is 26493 kWh, costing \$2649 at \$0.10/kWh
- Completely insulated (walls, ceiling, roof, best windows), get G<sub>tot</sub> = 118 W/K
  - four times better!
  - save \$2000 per cold season (and also save in warm season)

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